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THE LEAD TIME TRADE-OFF: THE CASE OF HEALTH STATES BETTER THAN DEATH

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ABSTRACT

The Lead Time Trade-Off (L-TTO) is a variant of the TTO method that tries to overcome some of the problems of the most widely used method (Torrance, 1986) for health states worse than death (SWD). Theoretically, the new method reduces the problems that have been detected when researchers have elicited preferences for SWD. However, several questions remain to be clarified. One of them is the influence of this new method for states better than death (SBD). In this paper we try to shed some light on this issue using a split sample design (n=500). One subsample (n=188) was interviewed using L-TTO and the rest using the traditional TTO (T-TTO). Our results show that the L-TTO produces utilities that are consistently higher than the T-TTO for SBD. Furthermore, the higher the severity the higher the difference between both methods. Another finding is that the L-TTO seems to produce a lower number of SWD. This effect seems to be concentrated in the most severe health states. This implies a violation of additive separability, one of the cornerstones of the QALY model. Our data show that the L-TTO may be different from the T-TTO in more respects than those that were originally intended.





Introduction

One of the main components of any Economic Evaluation of Health Care Programmes is the utility of health states. They are estimated using the Time Trade-Off (TTO) (Torrance, Thomas & Sackett, 1972) very often. Usually, utilities are elicited for chronic health states and they are applied to all sorts of health problems (chronic or temporary) and durations (long or short). Torrance (1986) presented two versions of TTO for chronic health states, one for SBD and one for SWD. The method Torrance (1986) proposed for SWD has been widely used (Tilling et al., 2010). A modified version of this method was used by the Eurogol Group in the UK Measurement and Valuation of Health (MVH) study (Dolan, 1997). However, it has been pointed out (Robinson & Spencer, 2006) that the framing used for SWD is very different from the framing used for SBD. In the case of SBD subjects are asked to trade-off more years in bad health with fewer years in better (or full) health. In the case of SWD they are asked to estimate the combination of years in full and bad health that is equivalent to death. Strictly speaking, if the assumptions of the QALY model would hold and subjects would have well-structured preferences for health problems, this change in framing should not be problematic. However, as Robinson and Spencer (2006, p. 394) say "there is a large body of evidence which shows that responses can be affected by simple variations in question wording -descriptive invariance- and the method used to elicit preferences -procedural invariance. Such evidence must call into question the validity of aggregating better than and worse than dead scores, generated by two different procedures". For these and other reasons it is perfectly reasonable to look at these two procedures as different "conceptually and operationally" (Devlin et al., 2011). Robinson and Spencer (2006) proposed a variant of the traditional TTO (from now on T-TTO), namely, the Lead TTO (L-TTO). The L-TTO includes a certain number of years (L) in full health before the period in bad health. In L-TTO we estimate utilities for SBD and SWD using the same procedure, that is, subjects have to say if they want to live longer with lower quality of life or viceversa.

However, the main reason to use L-TTO instead of T-TTO for SWD cannot just be that it avoids procedural invariance. If two procedures produce different results we cannot *solve* the problem choosing one them at random. The ultimate reason to choose L-TTO to elicit





preferences for SWD has to be that utilities elicited with L-TTO are closer to what we can call the "true" utility. Tilling et al. (2010) and Devlin et al. (2011) provide some reasons that can be interpreted as a justification that utilities elicited with L-TTO are closer to "true" preferences or, equivalently, that T-TTO produces biased utilities for SWD. They argue that T-TTO "produces 'extreme' negative values" (Devlin et al, 2011, p. 349) for SWD. The fact that T-TTO produces 'extreme' values is not a problem per se if they reflect what people really think. We understand that what they claim is that these "extreme negative values" do not reflect what people really think ("true" preferences). These values would be an artefact of the method. Also, they claim (Devlin et al, 2011, p. 359) that it is easier for people to "flip' from positive to negative values without the focusing effect created by the introduction of a separate valuation procedure". They seem to suggest that this "focusing effect" produce biased utilities. In summary, the argument seems to be that utilities provided by L-TTO.

These arguments have a potential problem, namely, L-TTO and T-TTO could be producing different values for the same health state because the introduction of a lead period affects TTO in different ways than those initially envisaged. One possibility is that people may violate additive separability. If there are interactions between "disjoint time periods" (Wakker, 1996) adding a lead period can change the "true" utility of a health state. As Devlin et al. (2011. p.359) say "while the lead time TTO appears to have the potential to overcome the problems of conventional TTO in valuing SWD, its use relies on the assumption of additive separability". If this assumption does not hold, the "true" value of health states is bound to be different between T-TTO and L-TTO (U_{L-TTO}) for SWD better represents preferences than utilities elicited with T-TTO (U_{L-TTO}) since preferences are not constant. Another possibility also mentioned by Devlin et al (2011, p. 360) is that "the introduction of lead time pushes the state to be valued further into the future, potentially (depending on the durations involved) increasing the effect of time preference on values."

The objective of this paper is to find out to what extent the potential discrepancy between U_{L-TTO} and U_{T-TTO} can be attributed to violations of procedural invariance or to some other reason. We do this by focusing on SBD. Since the procedure used to elicit utilities for SBD





is the same under L-TTO and T-TTO no violations of procedure invariance can explain a potential discrepancy between L-TTO and T-TTO for SBD.

Comparing L-TTO and T-TTO

In the T-TTO, at least for the chronic case of SBD, the utility of a health state is obtained after establishing indifference between two health profiles. Each profile is characterized by a combination of quality of life and time. That is we get:

$$U(\mathbf{x},F; \text{ death})=U(\mathbf{t},B; \text{ death})$$
 [1]

Where, traditionally, F indicates full health, B is a SBD, x is the number of years in full health and t is life expectancy.

Usually t is fixed and x is adjusted (x < t) until indifference is reached. Under the usual scaling assumptions and applying the linear QALY model

$$U_{\text{T-TTO}}(B) = x/t.$$
 [2]

For SWD this method cannot be applied given that for these states there is no x>0 which verifies [1]. The method developed by Torrance (1986) for SWD (denoted by W) estimates $U_{T-TTO}(W)$ from next indifference:

$$U(\mathbf{x},F; (\mathbf{t-x}),W; \text{ death})=U(\text{ death})$$
[3]

as follows

$$U_{T-TTO}(W) = -x/(t-x)$$
 [4]

It is clear that [1] and [3] imply a very different task for the subject so descriptive and procedural invariance can be easily violated. The L-TTO includes a certain number of years (L) in full health before the period in bad health (H). That is, U_{L-TTO} (H) is obtained by establishing indifference between next two profiles:





 $U(\mathbf{L},F;\mathbf{x},F;\text{death}) = U(\mathbf{L},F;\mathbf{t},H;\text{death})$

[5]

As it can be seen [1] and [5] are extremely similar. The only difference is that we add a common element (L,F) to both sides of the equation. Since the QALY model assumes additive separability, adding this common element makes no differences on the utility of H, that is U_{L-TTO} should be equal to U_{T-TTO} .

Let us define "y" such as y=L+x, that is, the number of years in full health that are equivalent to L years in full health plus t years in bad health. Equality [5] can then be written as

$$U(\mathbf{y},F;death) = U(\mathbf{L},F;\mathbf{t},H;death)$$
[6]

Under the linear QALY model and under the assumption of additive separability, U_{L-TTO} (H) is estimated as

$$U_{L-TTO}(H) = (y-L)/t$$
[7]

Observe than the framing in [6] can generate both positive and negative values for U_{L-TTO} (H). This was not possible under [1].

The procedure to elicit utilities for SBD is basically the same under T-TTO and L-TTO ([7] and [2] are both x/t). In both cases, the subject is asked to seek indifference between two health profiles, one of them with lower life expectancy and the other with lower quality of life. The only difference between both framings is the common lead-time period in full health that is added to both profiles. This leads to the main hypothesis we want to test in this paper, namely, that the only difference between T-TTO and L-TTO is the different procedure they use. In order to test this hypothesis we make two predictions:

- a. Utilities for SBD are not systematically different between T-TTO and L-TTO.
- b. The probability that a health state is considered better or worse than death does not change systematically between T-TTO and L-TTO.





If these hypotheses do not hold we will have evidence that the only difference between T-TTO and L-TTO is not the different procedure they use. If this were the case it would not be so straightforward to accept that utilities elicited with L-TTO for SWD are just the same utilities than the T-TTO tries to elicit but estimated with less bias. It could imply that the Lead period introduces other elements that modify the utilities estimated.

Two potential candidates that can introduce a discrepancy between U_{T-TTO} and U_{L-TTO} (apart from procedure) are violations of additive separability and discounting. If there are interactions between disjoint time periods the introduction of the lead time in full health can modify how people perceive the severity of a health state creating a discrepancy between U_{T-TTO} and U_{L-TTO}. However, there is no a theory that predicts the direction of this potential discrepancy. It is not the same with discounting. Under the constant discounting model (widely used in Economic Evaluation) the introduction of a lead-time period cannot explain any discrepancy between L-TTO and T-TTO since it assumes stationarity (see appendix). However, the literature has shown that this assumption is frequently violated and that temporal preferences can be better described assuming decreasing time aversion -DTA- (van der Pol and Cairns, 2002). In the appendix we show that these preferences could produce a discrepancy between U_{T-TTO} and U_{L-TTO} if responses to T-TTO and L-TTO are analysed using (wrongly) the linear QALY model. More specifically, we show that if U(Q) is constant across contexts $[U_{T-TTO}=U_{L-TTO}]$, temporal preferences are characterized by DTA and responses to T-TTO and L-TTO are analyzed using the linear QALY model we would get $U_{T-TTO}(Q) \le U_{L-TTO}(Q)$. We will see if this type of temporal preferences can explain our results.

In order to test our main hypothesis we conducted a survey in Galicia (North West of Spain) with 500 members of the general population. We now describe the survey and the statistical techniques. We then present the results and discussion closes the paper.

Methods

Selection of health states

The survey that we use in this study was funded mainly in order to estimate utilities for health states associated different levels of dependency generated by health problems. We





developed a descriptive system (Table 1) composed by six attributes with three or four levels per attribute. Five of the six attributes measure physical dependency and one measures mental problems¹. It gives rise to 1728 possible health states. The OPTEX Procedure from SAS Software (version 9.1) was used to generate a set of 24 health states divided into four blocks of size six (Table 2). Each participant in the survey valuated only one of the four blocks (6 health states). Blocks were randomly allocated among subjects. We also randomized order of presentation of health states. Each participant only used T-TTO or L-TTO, that is, we used a between sample design.

Selection of respondents

Subjects were selected using a four-stage cluster stratified random sampling with final adjustment to quotes by genre and age. The reference population was between 18 and 65 years old. We did not include older people because the life expectancy we used in the L-TTO (20 years) clearly exceeded their own. A total of 500 interviews were conducted: 312 participants responded the T-TTO protocol and 188 participants the L-TTO protocol. Interviews were conducted face-to-face by six trained interviewers.

The questionnaires

We use two types of questionnaires one for the T-TTO procedure developed by Torrance (1986) and another for the L-TTO procedure proposed by Robinson and Spencer (2006). Both types of questionnaire began motivating the study and explicating the health states (dimensions and levels) used in the questionnaire. Next, the subjects had to evaluate the six health states. We also collected the socio demographic characteristics of the participants: age, gender, family income, education, labour status, living arrangement, size of municipality, own health (measured by Euroqol EQ-5D), if they know a dependent relative and also if the relative lives with them.

Valuation procedure

¹ We focus here on the comparison between T-TTO and L-TTO. For this reason, we will not get into too many details of the origin of the health states we use in this paper. Very broadly: we developed a descriptive system based on some indexes widely used in the literature (Mahoney and Bartel, 1965; Katz et al., 1963; etc.), a descriptive analysis using the Spanish National Health Survey to joint in a more general description those attributes with a big correlation among them, and an interview with 5 experts in the valuation of dependency.





The procedure is illustrated in Figure 1. Subjects had to choose between two options (A and B) with different health profiles. Visual aids were used to help the subject understand these questions. The first question aimed to identify if health states were considered better or worse than death. In order to find this, in the case of the T-TTO, the first question involved choosing between death in a few weeks and 10 years in a certain health state. In the case of the L-TTO the first question involved choosing between (10 years full health; death) and (10 years in full health; 10 years in bad health; death).

Depending on the answer to the first question, the respondent followed a different path using a choice-bracketing procedure (series of ping-pong questions) as it is shown in Figure 1. In order to clarify our procedure we present two examples, one for the T-TTO and one for the L-TTO:

- T-TTO: Assume that somebody preferred (10 years, H; death) to death, then she would be asked to choose between (10 years, H; death) and (5 years, FH; death). The number of years in full health was moved up and down until an indifference interval (or value) was reached. When indifference was not directly obtained (most of the cases), we assigned the middle value of the indifference interval. For example, if (8 years, FH)≻ (10 years, H) and (7 years, FH) ≺(10 years, H) we assumed that (7.5 years, FH)~(10 years, H) and, applying equation [2], U(H)=.75. Figure 1 show (in the shaded areas) the values assigned to the health states depending on the path followed by subjects.
- L-TTO: Assume that somebody preferred (10 years, FH; 10 years, H) to (10 years, FH; death), then she would be asked to choose between (15 years, FH; death) and (10 years, FH; 10 years, H; death). Using the choice-bracketing technique shown for the T-TTO, we obtained an indifference (or value) interval. If (10 years, FH; 10 years, H; death) ~(12 years, FH ; death) applying equation [7] we would have that U(H)=0.2. Figure 2 show (in the shaded areas) the values assigned to the health states depending on the path followed by subjects.

Analysis

1. Consistency of the responses





We analyzed violations of dominance in order to test the consistency of responses. We considered that a health state dominates another one if it is at least better in one dimension and it is not worse off in any of the other dimensions. As it can be checked in table 2, there are several dominance situations (6 in the blocks 1-3 and 4 in the block 4 for a total of 22). For instance in block 1 the health state 313331 dominates 323433. We identified the number of participants who did not verify dominance at least once in both protocols.

2. Hypotheses testing

Our two hypotheses were tested as follows:

1. To test if the utilities for SBD depend on the protocol we formulated the following model:

$$U_{ij} = \alpha + \sum \beta_j s_j + \delta' x_i + \gamma Lead + \varepsilon_{ij}, \quad [8]$$

where U_{ij} is the utility assigned by respondent *i* to the health state *j* (*j* = 1, 2, ..., 24) if $U_{ij}>0$ (obtained applying the equation [2] for the T-TTO sample and the equation [7] for the L-TTO sample); s_j is a dummy variable indicating the state evaluated (e.g., $s_j = 1$ if *j*=1 and $s_j = 0$ if *j*≠1); x_i is a vector of personal characteristics of the participants; *Lead* is a dummy variable indicating if the participant used the L-TTO protocol (*Lead*=1) or the T-TTO protocol (*Lead*=0); *eij* is an error term and α , β_j , δ' and γ are the parameters to be estimated. This model was estimated using the random effects regression model because it takes into account that the same individual values several health states and then the observations provided the same participant cannot be considered independent. This model considers that $\varepsilon_{ij} = u_j + e_{ij}$ where u_j is the individual specific error term and e_{ij} is the traditional error term associated to each observation. We test if γ is statistically different from zero to test if L-TTO and T-TTO produce systematically different results.

2. To test if the probability that a health state is considered better or worse than death changes or not systematically between T-TTO and L-TTO, we estimate a random





effect logit model. The independent variables are the same as in [8]. The dependent variable is binary, taking a value of 1 if the respondent considers this state worse than death and 0 otherwise. We estimated a random-effects logit model in order to capture unobserved factors specific to each respondent. Finally we test if γ is statistically different from zero to analyze if the format used affects to the probability that a state will be considered worse or best than death.

Results

Table 3 shows the characteristics of respondents in both L-TTO and T-TTO samples. Both samples present similar socioeconomics characteristics and seem to have similar preferences regarding the importance of attributes. We have two fairly homogeneous samples. This suggests that our results regarding comparison between both methods can be robust. In any case, statistical analysis conducted controlled for potential differences between samples.

First of all we tested the consistency of the responses. This was done analyzing dominance. Since there are 22 pairwise combinations of states where one states dominated the other (it as not worse in any dimension and it was better in some other(s) dimension (s)) we tested if the parameters were significantly different from each other in these pairwise comparisons. The hypothesis of equality of parameters is rejected at 5% level in 18 pairs of states and always in the right direction, that is, the parameter associated with the dominant health state was always higher.

The main results regarding our two hypotheses can be seen in Table 4. In both cases we run two regressions excluding (models 1 and 4) or including (models 2 and 5) personal characteristics². Hypothesis 1 is clearly rejected in both models (see model 1 and 2). The coefficient of the *Lead* variable is positive and significantly different from cero. It is also quite high since the L-TTO adds about 0.2 points to the average utility of health states, regarding to the T-TTO method. Since we are dealing with states that move between 0 and 1 this is a very important effect.

 $^{^2}$ Income was excluded from our analysis because 9.6% of subjects did not respond to this question. We estimated the models including this variable and results did not change.





As mentioned in the section 2 (and shown in the appendix) our results could be explained by DTA. If we assume (erroneously) a linear QALY model and temporal preferences are characterized by DTA we would get U_{T-TTO}<U_{L-TTO} even if they are really the same. Therefore we should test if applying a DTA model these differences are eliminated. We used Harvey (1986) and Mazur (1987) models since they have been used in the health economics literature (Van Der Pol & Cairns, 2002). In Harvey (1986) we have that $\delta_t=1/(1+t)^h$ and in Mazur (1987) $\delta_t=1/(1+gt)$. We estimated utilities using these two models and the parameters estimated by Van Der Paul and Cairns (2002). The coefficient of the *Lead* variable was 0.15, that is smaller that previously estimated but still it was statistically significant at the 1% level and quite large. We conducted a sensitivity analysis using a wide of range of values for parameters *g* and *h* the parameter was statistically different from zero. In summary, discounting does not seem to be the fundamental explanation of the difference between T-TTO and L-TTO. We are left with violations of additive separability as the main candidate.

If the explanation of our result is that there are interactions between disjoint time periods it seems logical to think that this effect may depend on the severity of the health state. In order to test this hypothesis health states were divided in three groups according to severity. Each group had 8 health states: the less severe states were in group 1 and the most severe ones in group 3. The severity of a state was approximated according to the proportion of participants that consider the state as better or worse than dead in the T-TTO. Although it seems natural to identify the severity according to the utility of the health state this had the problem that for some health states the number of observations was small since most people considered the state as worse than death. Model 3 shows that the differences between L-TTO and T-TTO increases with severity. There are significant differences (Wald test) between the parameters of groups 1 and 2 and 1 and 3 at the 5% level and between groups 2 and 3 at the 10% level.

Hypothesis 2 cannot be rejected in any of the two models for the whole sample. The *Lead* variable is not significantly different from zero in model 4 and 5, indicating that the probability that a state is considered worse or better than death is not different between the T-TTO and the L-TTO. However, model 6 shows that the probability that a health state is considered worse than death is lower with L-TTO for the most severe health states. Adding a lead-time seems to have a special influence on the utility of the most severe health states.





This result also seems to support the conclusion that the disparity between T-TTO and L-TTO can be produced by a violation of additive separability since discounting cannot change the consideration of a health state as better or worse than death.

We also conducted other auxiliary regressions (results not shown) in order to test the stability of our results. Including sociodemographic variables, including and excluding missing values related with income and excluding participants who failed dominance at least once did not change the main results.

Discussion

The main results of this study are that: a) L-TTO seems to produce higher utilities than T-TTO for SBD, b) this effect seems to increase with severity, c) the probability that a heath state is considered as better or worse than death is only different between both methods for the most severe states, between those SBD. We conclude that the L-TTO and the T-TTO produce different utilities for SBD.

These results seem to reflect a violation of the principle of additive separability, that is, people perceive health states differently if a lead period in full health is added upfront. There is nothing wrong in violating this assumption. It is a convenient assumption (makes the QALY model more tractable) but it is not a normative assumption. As Wakker (1996) has pointed out, QALY assumptions can only be expected to hold approximately and "whether the greater tractability of analysis outweighs the loss of empirical realism is a question that cannot be answered in a universal manner; the answer depends on context and application" (p. 209). In our context assumption additive separability seems to have a high cost in terms of empirical realism.

One explanation of this result is that the introduction of a lead period in full health allows people to prepare for the bad years that will come. While in T-TTO the bad years are a surprise (they start immediately) in L-TTO people have time to make adjustments. If 10 healthy years are added upfront, a person can during those 10 years take preparations for what is to come after, reducing burdens and hence diminishing differences. The important jobs to be done before the trouble starts can now be taken care of before. This is a kind of interaction between disjoint time periods that is very natural. If this is true, the





consequence is that the "true" utility that T-TTO and L-TTO elicit is intrinsically different. For this reason, if both methods produce different results for SWD we cannot conclude that L-TTO produce utilities that are closer to "true" values since it seems that "true" values are different. They are context-dependent. For example, in those contexts where illnesses are diagnosed in advance and symptoms do not show up immediately (e.g. Parkinson), utilities elicited with L-TTO can be closer to "true" preferences.

As far as we know, there are at least two more studies that have presented some evidence on the issues that we have explored in this paper. Devlin et al. (2011) interviewed a group of 109 subjects from the general population using the L-TTO. They compared their results with those of the MVH study and their conclusions were similar to ours. That is, they found that L-TTO and T-TTO produced comparable proportion of respondents considering a health state better or worse than death in 7 out 10 states. In those states where there were significant differences, for the two more severe states (EQ-5D 13332 and EQ-5D 23232) L-TTO produced a lower proportion of respondents considering this state worse than death and the opposite occurs for the less severe state (EQ-5D 11112). Also, they found that in four of the 10 health states analysed, the L-TTO produced higher utilities than T-TTO for SBD. Attema et al (2011) also compared T-TTO and L-TTO. They evaluated only six health states but they used several lead time. They show that the utility of health states depend on the lead time. Utilities were lower for shorter lead time (5 years) than for longer (10 and 17 years) in the case of SBD. This represents another violation of additive independence. In order to compare with our results, we will only focus on their results corresponding to the lead time that we used (10 years). Unfortunately, they only used 3 health states with this lead time and their results are inconclusive. For the mildest health state (EQ-5D 11121) the mean (and median) utility of T-TTO was higher than the utility of L-TTO and for the intermediate health state (EQ-5D 11113) and the worse health state (EQ-5D 23232) L-TTO produced a higher value than T-TTO (the medians were the same in the intermediate state and higher in the L-TTO for the worse state).

There is a message that seems to come from these studies that have used L-TTO, namely, utilities are not constant across contexts. The ultimate solution to this problem is to try to understand how context influence utilities and use those values that better represent preferences in each context. However, this can be (or not) considered unfeasible and unrealistic. In the meantime, utilities have to be used in decision making. A decision has to





be taken if we go on with T-TTO or we move to L-TTO. Robinson and Spencer (2006) and Devlin et al (2011) have presented some arguments in favour of the L-TTO. What our paper suggests is that if L-TTO is going to substitute T-TTO this would not only affect SWD but also SBD and a whole new set of values will have to be produced. These utilities will not just be better estimations of the same "true" values formerly elicited with T-TTO but a whole set of "new true values".

Our paper also has limitations that should be overcome in future research. We have compared both methods in a between-sample design. While we think this is the best design in order to test if both methods produce different utilities, it is not the best method in order to understand why T-TTO and L-TTO produce different results. This can be better addressed in a within-sample design. Of course, a within-sample design may have confounding factors of its own that will have to be carefully controlled (e.g. order and learning effects) but it seems the right design in order to understand the reason of the discrepancy. Another limitation of our study is that subjects were not randomised between both methods. Administrative and organizational issues made randomization impossible. Since the sociodemographic characteristics of both samples were quite similar and since we used multivariate analysis in order to control for biases coming from nonrandomization we do not think there are obvious reasons to suspect that our results are biased.

Recently Devlin et al., (2011. p. 348) suggested that one topic for further research with L-TTO was "to better understand the implications for valuations of states better than dead". Our paper is an attempt to fill this gap. Further research should try to understand why adding a common outcome or why changing the size of this common outcome to health profiles seems to influence so heavily the utilities elicited.





Appendix

Effect of discounting in T-TTO and L-TTO for SBD.

Assume somebody is indifferent between Y years in Full Health (FH) and T years in health state Q (Y<T, Q<FH), under T-TTO. The utility of Q would be estimated as

$$U_{T-TTO}(Q) = \frac{(\delta_1 + \dots + \delta_Y)}{(\delta_1 + \dots + \delta_Y + \dots + \delta_T)} \quad 0 < \delta_t < 1$$
 [1a]

where δ_t is the weight associated to one life year that occurs in the period t (δ_t =1 for the linear QALY model).

In L-TTO we add a common delay L in full health to both profiles. Utility is estimated as

$$U_{L-TTO}(Q) = \frac{\left(\delta_{L+1} + \dots + \delta_{L+Y}\right)}{\left(\delta_{L+1} + \dots + \delta_{L+Y} + \dots + \delta_{L+T}\right)}$$
[2a]

Under the constant discounting model the *relative* benefit of receiving one outcome sooner (*t*) or later (*t'*) only depends on the absolute distance between *t* and *t'*. That is, if we delay *t* and *t'* by a common period L, we have that

$$\frac{\delta_{e}}{\delta_{e'}} = \frac{\delta_{2+e}}{\delta_{L+e'}}$$

Given that under constant discounting $\delta_{L+t} = \delta_L x \delta_t$, then [3a]=[3b]. That is U_{T-TTO}(Q)=U_{L-TTO}(Q)

2. Under a decreasing discount the effect of a delay L (δ_L) is not constant but it increases with the moment in time it is produced. That is, if t'>t we have that

$$\frac{\delta_{c'}}{\delta_c} < \frac{\delta_{L+c'}}{\delta_{L+c}}$$





Therefore

 $\sum_{k=1}^{Y} \frac{1}{\delta_{t}} \left[\sum_{k'=1}^{T} \delta_{t'} \right] < \sum_{k=1}^{Y} \frac{1}{\delta_{t+s}} \left[\sum_{k'=1}^{T} \delta_{t'+s} \right] \rightarrow \frac{\sum_{t=1}^{X} \delta_{t}}{\sum_{t'=1}^{T} \delta_{t'}} > \frac{\sum_{t=1}^{X} \delta_{t+s}}{\sum_{t'=1}^{T} \delta_{t'+s}}$

That is $U_{T-TTO}(Q)>U_{L-TTO}(Q)$. Therefore if a subject gives up the same number of life years in full health in T-TTO than in L-TTO and she has temporal preferences characterized by DTA she would be implying that $U_{T-TTO}(Q)>U_{L-TTO}(Q)$.

Assume that somebody has preferences such that U(Q) is constant across contexts, that is, $U_{T-TTO}(Q)=U_{L-TTO}(Q)$ and she has temporal preferences characterized by DTA. In this case she would give up less life years in L-TTO than in T-TTO. If this were the case and we would analyze T-TTO and L-TTO responses using the linear QALY model then we would find that $U_{T-TTO}(Q) < U_{L-TTO}(Q)$.





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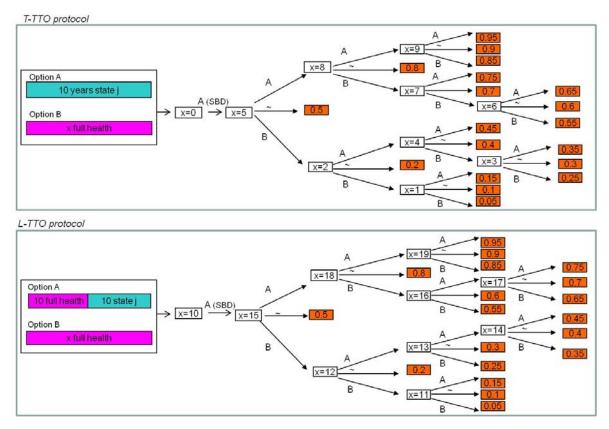
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Figure 1: Protocol used in the questionnaire: T-TTO version and L-TTO version







Tuble 1. Depende	Tuble 1. Dependency states. Difer description of attributes and revers				
Eat	 Does not need assistance to eat or drink. Needs partial aid to eat or drink (cutting, serving, etc.). Needs to be given food and drink. 				
Incontinence	 Does not have incontinence or does not need help. Has urinary incontinence (not fecal) and needs help for hygiene. Has both urinary and fecal incontinence and needs help for hygiene. 				
Personal care	 Does not need help for personal care: bathing, dressing, etc. Needs help only to bath but not for the rest of his/her personal care. Needs help for most personal care activities. Is incapable of carrying out personal care. Needs someone to substitute him/her in this activity. 				
Mobility	 Moves independently. Does not need help to move within the home but does out of home. Needs help to move both in and out of home. Is incapable of changing position. Bed-ridden or chair-ridden. 				
Housework	 Does not need help to carry out housework (cleaning, food, etc.). Needs daily help for housework. Is incapable of carrying out most tasks at home. 				
Mental problems	 Does not have mental impairment. Is not mentally impaired. Needs assistance to manage money, medication or to take some common everyday decisions. Collaborative attitude with the care-taker. Incapable of taking basic decisions. Cannot live alone. Does not collaborate but does not offer resistance. Incapable of taking basic decisions. Does not collaborate and usually offers resistance to help. 				

Table 1: Dependency states. Brief description of attributes and levels





Table 2: Dependency states evaluated by block*					
	211121		111112		
	133334		113233		
Block 1	122222	Block 3	213322		
	214232		222131		
	313331		234431		
	323433		334234		
	111221		123121		
	112132		212223		
Block 2	112211	Block 4	233432		
	223234		314434		
	234333		324332		
	333122		333231		

* The number indicates the level of each attribute following the order of the Table 1.





		L-TTO	T-TTO
		N=188	N=312
Sex	Female	55.8	47.4
Age	Mean	40.9	41.5
	Primary studies or less	35.1	37.5
Education	Secondary	37.2	39.4
	University	27.7	23.1
	Rural	34.6	31.4
Habitat	Intermediate	29.3	31.1
	Urban	36.2	37.5
Living alone		9.7	13.5
Good health	(EQ-5D=11111)	68.6	76.3
	Any close dependent	31.4	53.2
Know	Close dep. (not live together)	59.0	40.1
	Close dep. (live together)	9.6	6.7
	Employed	58.0	59.6
	Pensioner/retired	6.4	10.9
Labour status	Unemployed	23.4	16.0
	Student	6.4	5.1
	Domestic tasks	5.9	8.3
	<=500	6.1	5.9
	500-1000	23.9	13.2
Home income	1000-1500	25.0	30.5
€ monthly)	1500-2000	16.7	25.7
	2000-3000	20.0	16.9
	>3000	8.4	7.7
Duration of interview (minutes)		22.5	23,2
	Eat	4.8	8.0
	Incontinence	5.9	7.1
Participants	Personal care	4.3	6.7
who placed it in first place	Mobility	7.5	8.7
in mot place	Housework	0.0	0.3
	Mental	77.7	69.2
	Eat	16.49	16.99
	Incontinence	45.21	30.13
Participants	Personal care	10.11	19.55
who placed it in second place	Mobility	15.43	20.19
in second place	Housework	2.13	2.88
	Mental	10.64	10.26

Table 3: Characteristics of respondents by type of questionnaire (%)





Table 4: Results of the estimation

	Hypothesis 1			Hypothesis 2 Bandom Logit model		
	Random regression model Model 1 Model 2 Model 3		Random Logit model Model 4 Model 5 Model 6			
Constant	Model 1					
	0,637**	0,646**	0,651**	-4,596**	-6,544**	-4,786**
States [Ref: 211121]	0.040**	0.047**	0.215**	C 0 4 C **	(025**	7 45244
133334	-0,249**	-0,247**	-0,315**	6,946**	6,935**	7,453**
122222	-0,196**	-0,195**	-0,195**	2,741**	2,718**	2,755**
214232	-0,186**	-0,184**	-0,215**	3,650**	3,619**	3,768**
313331	-0,130**	-0,128**	-0,161**	3,032**	3,006**	3,149**
323433	-0,252**	-0,251**	-0,324**	6,682**	6,665**	7,183**
111221	0,048	0,053	0,049	0,218	0,155	0,173
112132	-0,096**	-0,091**	-0,095**	2,013**	1,965**	1,975**
112211	0,015	0,020	0,017	0,218	0,155	0,173
223234	-0,233**	-0,229**	-0,300**	6,769**	6,709**	7,299**
234333	-0,299**	-0,294**	-0,368**	6,330**	6,274**	6,853**
333122	-0,200**	-0,195**	-0,231**	5,767**	5,716**	5,855**
111112	-0,041	-0,041	-0,037	1,052	0,916	0,981
113233	-0,171**	-0,171**	-0,202**	5,046**	4,927**	5,106**
213322	-0,206**	-0,206**	-0,237**	4,780**	4,661**	4,840**
222131	-0,146**	-0,146**	-0,144**	2,778**	2,655**	2,708**
234431	-0,248**	-0,250**	-0,280**	6,498**	6,390**	6,558**
334234	-0,271**	-0,272**	-0,330**	7,500**	7,407**	8,071**
123121	-0,098**	-0,096**	-0,096**	2,143**	2,200**	2,095**
212223	-0,142**	-0,138**	-0,176**	5,348**	5,427**	5,431**
233432	-0,185**	-0,182**	-0,247**	6,713**	6,790**	7,258**
314434	-0,191**	-0,188**	-0,258**	7,877**	7,954**	8,436**
324332	-0,188**	-0,184**	-0,242**	6,618**	6,695**	7,162**
333231	-0,151**	-0,148**	-0,187**	5,194**	5,274**	5,277**
Lead [Ref: T-TTO]	0.179**	0.204**	•, - • ,	-0.400	-0.498	-,
Lead2 [Ref: T-TTO]						
Group 1 (less severe)			0.136**			0.230
Group 2 (intermediate)			0.227**			-0.084
Group 3 (more severe)			0.281**			-1.298**
Sex [Ref: female]		-0.041	0.201		-0.059	1.290
Age		0.001			0.013	
Education [Ref: primary]		0.001			0.015	
Secondary		0.006			-0.051	
-		-0.065*			0.257	
University Habitat [Ref: rural]		-0.005			0.237	
		0.050			1 211**	
Intermediate		-0.050			1.311**	
Urban		0.025			1.298**	
Living alone [Ref:No]		0.013			0.065	
Know [Ref: Any close]		0.070**			0.050	
Not live together.		-0.079**			0.350	
Live together.		-0.140**			0.068	
Good health		0.026			0.0(0)	
[Ref: EQ-5D≠11111]		0.036			0.269	
Labour status [Ref:employ.]		0.011			0.425	
Pensioner/retired		-0.041			-0.435	
Unemployed		0.026			0.676*	
Student		-0.055			0.770	
Domestic tasks		0.066			0.071	
Respondents	456	456		500	500	
Observations	1557	1557		3000	3000	

**Significant at the 5% level; *significant at the 10% level